

MR2928430 (Review) 53C40

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Weingarten spacelike hypersurfaces in a de Sitter space. (English summary)

An. Științ. Univ. "Ovidius" Constanța Ser. Mat. **20** (2012), *no. 1*, 387–406.1844-0835

In this article the authors study spacelike hypersurfaces M^n in an $(n+1)$ -dimensional de Sitter space $S_1^{n+1}(1)$. More precisely, they consider two classes of hypersurfaces M^n which have two distinct principal curvatures. On the one hand, they examine hypersurfaces which satisfy a linear Weingarten relation $\alpha R + \beta H + \gamma = 0$ where R is the scalar curvature, H is the mean curvature and α, β and γ are constants such that $\alpha^2 + \beta^2 \neq 0$. These hypersurfaces are called linear Weingarten spacelike hypersurfaces. On the other hand, hypersurfaces for which $\rho^2 = S - nH^2$ is a nonzero constant are studied. Here S is the square of the length of the second fundamental form. These hypersurfaces are called constant ρ Weingarten spacelike hypersurfaces.

Several lemmas that are used to obtain two classification theorems of linear Weingarten spacelike hypersurfaces and of constant ρ Weingarten spacelike hypersurfaces are stated, some of them with a proof. The classification theorems contain the Riemannian product $H^k(1 - \coth^2 \varrho) \times S^{n-k}(1 - \tanh^2 \varrho)$, where $1 < k < n-1$, the hyperbolic cylinder $H^1(1 - \coth^2 \varrho) \times S^{n-1}(1 - \tanh^2 \varrho)$ and the spherical cylinder $H^{n-1}(1 - \coth^2 \varrho) \times S^1(1 - \tanh^2 \varrho)$.

Reviewed by [Wendy Goemans](#)

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